#### Script generated by TTT

Title: Sturm: Visual Navigation (26.06.2012)

Date: Tue Jun 26 10:18:22 CEST 2012

Duration: 89:39 min

Pages: 97



#### **Exercise Sheet 5**

- Prepare mid-term presentation
- Proposed structure: 3 slides
  - 1. Remind people who you are and what you are doing (can be same slide as last time)
  - 2. Your work/achievements so far (video is a plus)
  - 3. Your plans for the next two weeks
- Hand in slides before July 3, 10am





# **Visual Navigation for Flying Robots**

# Place Recognition, ICP, and Dense Reconstruction

Dr. Jürgen Sturm



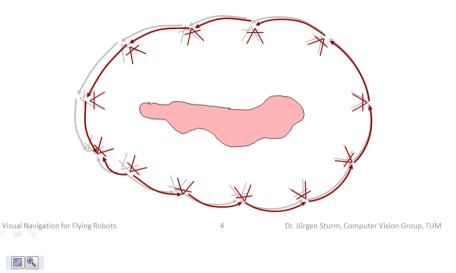
#### **Agenda for Today**

- Localization
  - Visual place recognition
  - Scan matching and Iterative Closest Point
- Mapping with known poses (3D reconstruction)
  - Occupancy grids
  - Octtrees
  - Signed distance field
  - Meshing



# **Remember: Loop Closures**

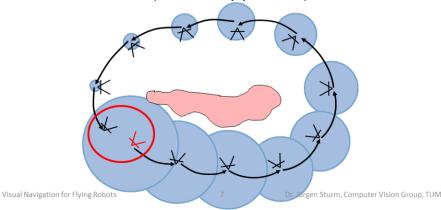
Use loop-closures to minimize the drift / minimize the error over all constraints



# **Loop Closures**

How can we detect loop closures efficiently?

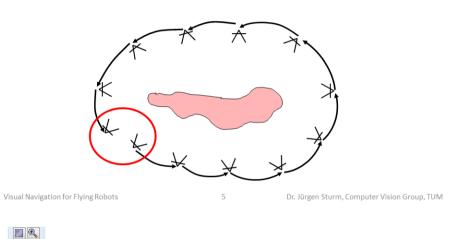
2. Use motion model and covariance to limit search radius (metric approach)





#### **Loop Closures**

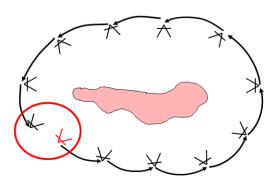
How can we detect loop closures efficiently?



# **Loop Closures**

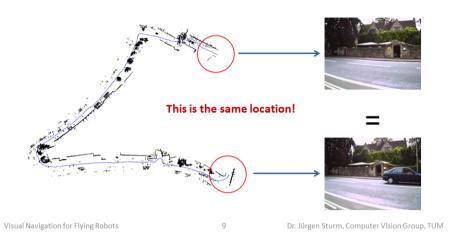
How can we detect loop closures efficiently?

3. Appearance-based place recognition (using bag of words)



# **Appearance-based Place Recognition**

Appearance can help to recover the pose estimate where metric approaches might fail





# **Object/Scene Recognition**

Analogy to documents: The content can be inferred from the frequency of visual words

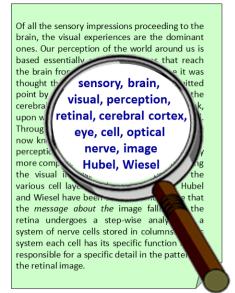


object



bag of visual words

#### **Analogy to Document Retrieval**



China is forecasting a trade surplus of \$90bn (£51bn) to \$100bn this year, a threefold increase on 2004's \$32bn. The Commerce Ministry said the surpl predicted 309 China, trade. surplus, commerce, which unfair exports, imports, US, vuan yuan, bank, domestic, says th foreign, increase, trade, value so more g increased within a narrow band, yuan to be allowed to trade freely Beijing has made it clear that it will tak and tread carefully before allowing the rise further in value.

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#### **Bag of Visual Words**

Visual words = (independent) features







### **Bag of Visual Words**

- Visual words = (independent) features
- Construct a dictionary of representative words

#### dictionary of visual words (codebook)

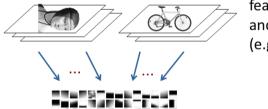


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#### **Overview**



feature detection and extraction (e.g., SIFT, ...)



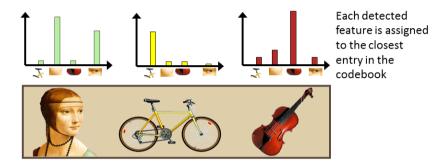
codewords dictionary



image representation (histogram of word occurrences)

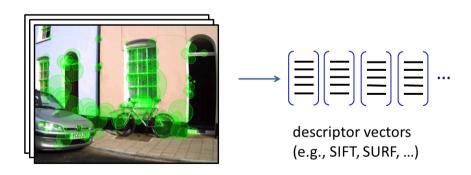
### **Bag of Visual Words**

- Visual words = (independent) features
- Construct a dictionary of representative words
- Represent the image based on a histogram of word occurrences (bag)

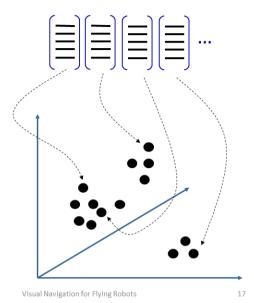




## **Learning the Dictionary**



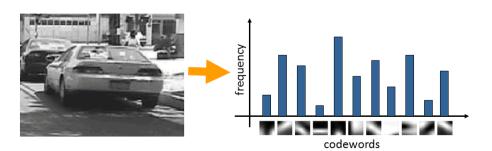
# **Learning the Dictionary**



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## **Example Image Representation**

Build the histogram by assigning each detected feature to the closest entry in the codebook





#### **Learning the Visual Vocabulary**



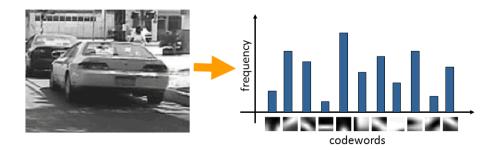
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## **Example Image Representation**

Build the histogram by assigning each detected feature to the closest entry in the codebook

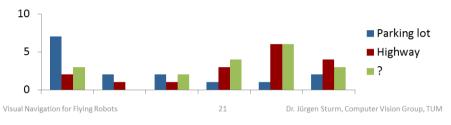


### **Object/Scene Recognition**

- Compare histogram of new scene with those of known scenes, e.g., using
  - simple histogram intersection

$$score(\mathbf{p}, \mathbf{q}) = \sum \min(p_i, q_i)$$

- naïve Bayes
- more advanced statistical methods



# **Example: FAB-MAP**

[Cummins and Newman, 2008]



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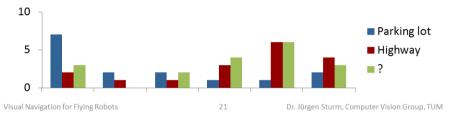


#### **Object/Scene Recognition**

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- naïve Bayes
- more advanced statistical methods





#### **Example: FAB-MAP**

[Cummins and Newman, 2008]





#### **Example: FAB-MAP**

[Cummins and Newman, 2008]





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#### **Summary: Bag of Words**

[Fei-Fei and Perona, 2005; Nister and Stewenius, 2006]

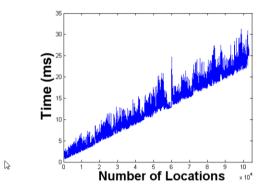
- Compact representation of content
- Highly efficient and scalable
- Requires training of a dictionary
- Insensitive to viewpoint changes/image deformations (inherited from feature descriptor)

.



# **Timing Performance**

- Inference: 25 ms for 100k locations
- SURF detection + quantization: 483 ms



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#### **Laser-based Motion Estimation**

- So far, we looked at motion estimation (and place recognition) from visual sensors
- Today, we cover motion estimation from range sensors
  - Laser scanner (laser range finder, ultrasound)
  - Depth cameras (time-of-flight, Kinect ...)









#### **Laser Scanner**

Measures angles and distances to closest obstacles

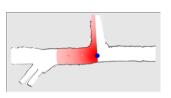
$$\mathbf{z} = (\theta_1, z_1, \dots, \theta_n, z_n) \in \mathbb{R}^{2n}$$

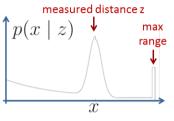
Alternative representation: 2D point set (cloud)

$$\mathbf{z} = (x_1, y_1, \dots, x_n, y_n)^{\top} \in \mathbb{R}^{2n}$$

• Probabilistic sensor model  $p(z \mid x)$ 







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#### **Exhaustive Search**

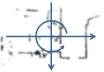
Convolve first scan with sensor model



 Sweep second scan over likelihood map, compute correlation and select best pose









#### **Laser-based Motion Estimation**

How can we best align two laser scans?

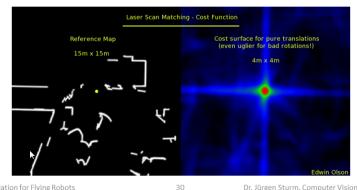
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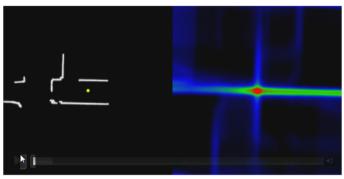
# **Example: Exhaustive Search** [Olson, '09]

- Multi-resolution correlative scan matching
- Real-time by using GPU
- Remember: SE(2) has 3 DOFs



#### **Example: Exhaustive Search** [Olson, '09]

- Multi-resolution correlative scan matching
- Real-time by using GPU
- Remember: SE(2) has 3 DOFs



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#### **Does Exhaustive Search Generalize To 3D As Well?**

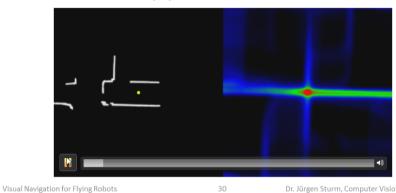






#### **Example: Exhaustive Search** [Olson, '09]

- Multi-resolution correlative scan matching
- Real-time by using GPU
- Remember: SE(2) has 3 DOFs



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# **Iterative Closest Point (ICP)**

Given: Two corresponding point sets (clouds)

$$P = \{\mathbf{p}_1, \dots, \mathbf{p}_n\}$$
$$Q = \{\mathbf{q}_1, \dots, \mathbf{q}_n\}$$

Wanted: Translation t and rotation R that minimize the sum of the squared error

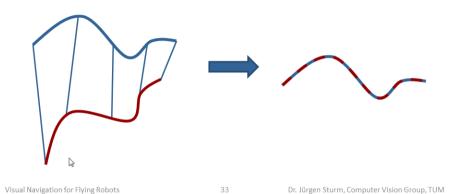
$$E(R, \mathbf{t}) = \frac{1}{n} \sum_{i=1}^{n} ||\mathbf{p}_i - R\mathbf{q}_i - \mathbf{t}||^2$$

where  $p_i$  and  $q_i$  are corresponding points



#### **Known Correspondences**

**Note:** If the correct correspondences are known, both rotation and translation can be calculated in **closed form**.





#### **Known Correspondences**

Decompose the matrix

$$W = \sum_{i} (\mathbf{p}_i - \bar{\mathbf{p}})(\mathbf{q}_i - \bar{\mathbf{q}})^{\top} = USV^{\top}$$

using singular value decomposition (SVD)

Theorem

If  $\operatorname{rank} W = 3$ , the optimal solution of  $E(R, \mathbf{t})$  is unique and given by

$$R = UV^{\top}$$
$$\mathbf{t} = \bar{\mathbf{p}} - R\bar{\mathbf{q}}$$

(for proof, see http://hss.ulb.uni-bonn.de/2006/0912/0912.pdf, p.34/35)



#### **Known Correspondences**

• Idea: The center of mass of both point sets has to match

$$\bar{\mathbf{p}} = \frac{1}{n} \sum_{i} \mathbf{p}_{i}$$
  $\bar{\mathbf{q}} = \frac{1}{n} \sum_{i} \mathbf{q}_{i}$ 

- Subtract the corresponding center of mass from every point
- Afterwards, the point sets are zero-centered, i.e., we only need to recover the rotation...

B

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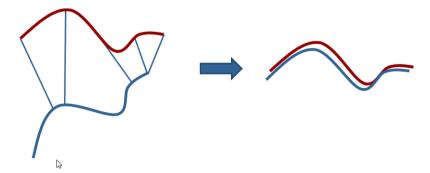
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#### **Unknown Correspondences**

 If the correct correspondences are not known, it is generally impossible to determine the optimal transformation in one step



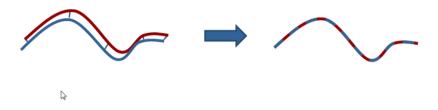
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# **ICP Algorithm**

[Besl & McKay, 92]

- Algorithm: Iterate until convergence
  - Find correspondences
  - Solve for R,t
- Converges if starting position is "close enough"

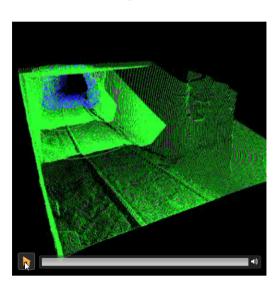


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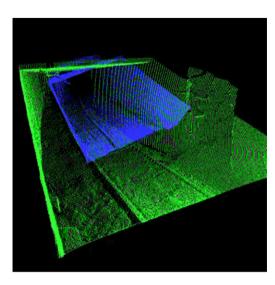


#### **Example: ICP**





#### **Example: ICP**



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#### **ICP Variants**

Many variants on all stages of ICP have been proposed:

- Selecting and weighting source points
- Finding corresponding points
- Rejecting certain (outlier) correspondences
- Choosing an error metric
- Minimization



#### **Performance Criteria**

- Various aspects of performance
  - Speed
  - Stability (local minima)
  - Tolerance w.r.t. noise and/or outliers
  - Basin of convergence (maximum initial misalignment)
- Choice depends on data and application

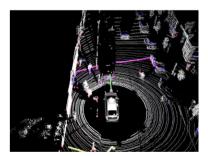
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# **Spatially Uniform Sampling**

- Density of points usually depends on the distance to the sensor → no uniform distribution
- Can lead to a bias in ICP





# **Selecting Source Points**

- Use all points
- Uniform sub-sampling
- Random sampling
- Feature-based sampling
- Normal-space sampling
  - Ensure that samples have normals distributed as uniformly as possible

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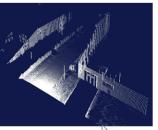
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#### **Feature-based Sampling**

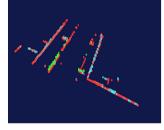
Detect interest points (same as with images)

- Decrease the number of correspondences
- Increase efficiency and accuracy
- Requires pre-processing



3D Scan (~200.000 Points)

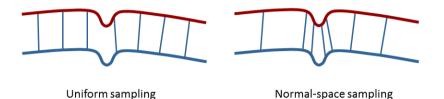
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Extracted Features (~5.000 Points)



### **Normal-Space Sampling**



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## **Selection and Weighting**

- Selection is a form of (binary) weighting
- Instead of re-sampling one can also use weighting
- Weighting strategy depends on the data
- Pre-processing / run-time trade-off



#### **Example: Normal-Space Sampling**

Normal-space sampling can help on mostlysmooth areas with sparse features



Random sampling



Normal-space sampling

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#### **Finding Correspondences**

Has greatest effect on convergence and speed

- Closest point
- Normal shooting
- Closest compatible point
- Projection
- Speed-up using kd-trees (or oct-trees)



#### **Closest Point Matching**

- Find closest point in the other point set
- Distance threshold



 Closest-point matching generally stable, but slow and requires pre-processing

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#### **Closest Compatible Point**

- Can improve effectiveness of both the previous variants by only matching to compatible points
- Compatibility based on normals, colors, ...
- In the limit, degenerates to feature matching



#### **Normal Shooting**

Project along normal, intersect other mesh



 Slightly better than closest point for smooth meshes, worse for noisy or complex meshes

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## **Speeding Up Correspondence Search**

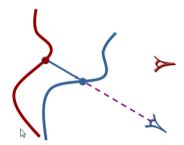
Finding closest point is most expensive stage of the ICP algorithm

- Build index for one point set (kd-tree)
- Use simpler algorithm (e.g., projection-based matching)



#### **Projection-based Matching**

- Slightly worse performance per iteration
- Each iteration is one to two orders of magnitude faster than closest-point
- Requires point-to-plane error metric



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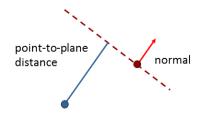
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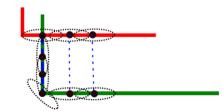
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#### **Error Metrics**

- Point-to-point
- Point-to-plane lets flat regions slide along each other



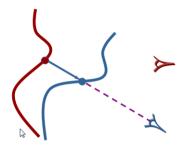


 Generalized ICP: Assign individual covariance to each data point [Segal, 2009]



### **Projection-based Matching**

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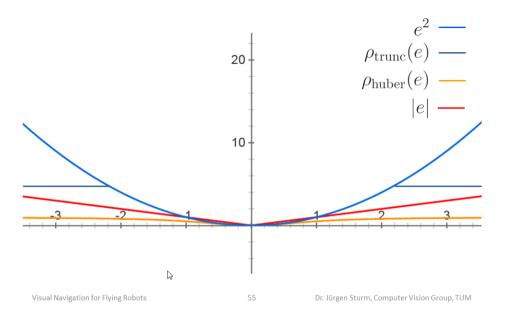


#### **Minimization**

- Only point-to-point metric has closed form solution(s)
- Other error metrics require non-linear minimization methods
  - Which non-linear minimization methods do you remember?
  - Which robust error metrics do you remember?



#### **Robust Error Metrics**





#### **ICP: Summary**

- ICP is a powerful algorithm for calculating the displacement between point clouds
- The overall speed depends most on the choice of matching algorithm
- ICP is (in general) only locally optimal → can get stuck in local minima



#### **Example: Real-Time ICP on Range Images**

[Rusinkiewicz and Levoy, 2001]

- Real-time scan alignment
- Range images from structure light system (projector and camera, temporal coding)





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#### **Agenda for Today**

- Localization
  - Visual place recognition
  - Scan matching and Iterative Closest Point
- Mapping with known poses (3D reconstruction)
  - Occupancy grids
  - Octtrees
  - Signed distance field
  - Meshing

No.



#### **Occupancy Grid**

#### Idea:

Represent the map m using a grid



• Each cell is either free or occupied

$$\mathbf{m} = (m_1, \dots, m_n) \in \{\text{empty}, \text{occ}\}^n$$

■ Robot maintains a belief Bel(m) on map state

**Goal:** Estimate the belief from sensor observations

$$Bel(\mathbf{m}) = P(\mathbf{m} \mid \mathbf{z}_1, \dots, \mathbf{z}_t)$$

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# **Mapping**

Goal: Estimate

$$Bel(m) = P(m \mid z_1, \dots, z_n)$$

How can this be computed?



#### **Occupancy Grid - Assumptions**

- Map is static
- Cells have binary state (empty or occupied)
- All cells are independent of each other
- As a result, each cell  $m_i$  can be estimated independently from the sensor observations
- Will also drop index i (for the moment)

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### **Binary Bayes Filter**

- Prior probability that cell is occupied P(m) (often 0.5)
- Inverse sensor model  $P(m \mid z_t)$  is specific to the sensor used for mapping
- The log-odds representation can be used to increase speed and numerical stability

$$L(x) := \log \frac{p(x)}{p(\neg x)} = \log \frac{p(x)}{1 - p(x)}$$



#### **Binary Bayes Filter**

- Prior probability that cell is occupied P(m) (often 0.5)
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$$L(x) := \log \frac{p(x)}{p(\neg x)} = \log \frac{p(x)}{1 - p(x)}$$

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# **Clamping Update Policy**

- Often, the world is not "fully" static
- Consider an appearing/disappearing obstacle
- To change the state of a cell, the filter needs as many positive (negative) observations
- Idea: Clamp the beliefs to min/max values

$$L'(m \mid z_{1:t}) = \max(\min(L(m \mid z_{1:t}), l_{\max}), l_{\min})$$

R



### **Binary Bayes Filter using Log-Odds**

In each time step, compute

previous belief sensor model map prior 
$$L(m \mid z_{1:t}) = L(m \mid z_{1:t-1}) + L(m \mid z_{t}) + L(m)$$

When needed, compute current belief as

$$Bel_t(m) = 1 - \frac{1}{1 + \exp L(m \mid z_{1:t})}$$

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#### **Sensor Model**

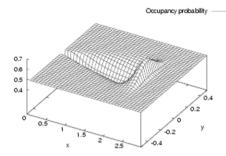
 For the Bayes filter, we need the inverse sensor model

$$p(m \mid z)$$

- Let's consider an ultrasound sensor
  - Located at (0,0)
  - Measures distance of 2.5m
  - How does the inverse sensor model look like?

# **Typical Sensor Model for Ultrasound**

 Combination of a linear function (in xdirection) and a Gaussian (in y-direction)



• Question: What about a laser scanner?

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## **Resulting Map**

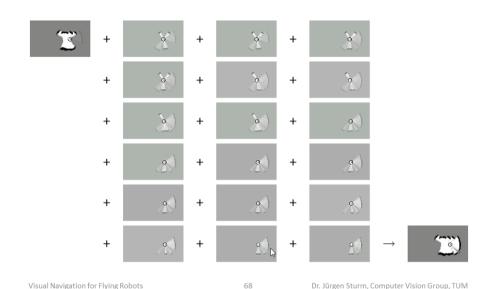




**Note:** The maximum likelihood map is obtained by clipping the occupancy grid map at a threshold of 0.5



#### **Example: Updating the Occupancy Grid**



**•** 

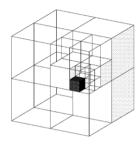
# **Memory Consumption**

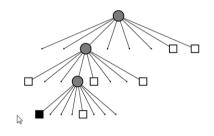
- Consider we want to map a building with 40x40m at a resolution of 0.05cm
- How much memory do we need?



### **Map Representation by Octtrees**

- Tree-based data structure
- Recursive subdivision of space into octants
- Volumes can be allocated as needed.
- Multi-resolution





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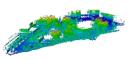
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#### **Example: OctoMap**

[Wurm et al., 2011]

 Freiburg computer science campus 292 x 167 x 28 m<sup>3</sup>, 0.2m resolution, 2mb on disk

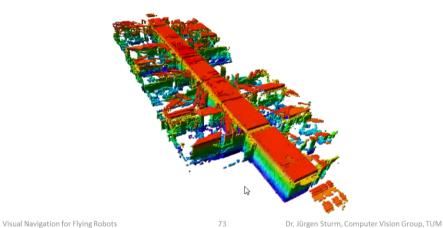




#### **Example: OctoMap**

[Wurm et al., 2011]

Freiburg, building 79 44 x 18 x 3 m<sup>3</sup>, 0.05m resolution, 0.7mb on disk

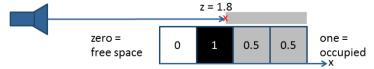




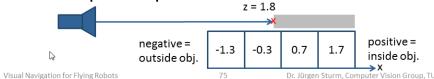
#### **Signed Distance Field (SDF)**

[Curless and Levoy, 1996]

- Idea: Instead of representing the cell occupancy, represent the distance of each cell to the surface
- Occupancy grid maps: explicit representation



SDF: implicit representation

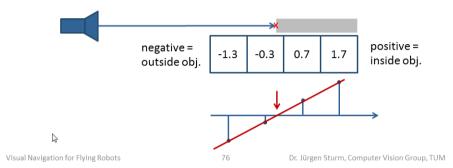


### **Signed Distance Field (SDF)**

[Curless and Levoy, 1996]

#### Algorithm:

- 1. Estimate the signed distance field
- 2. Extract the surface using interpolation (surface is located at zero-crossing)



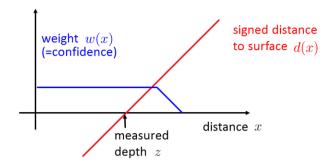
#### **Data Fusion**

- Each voxel cell x in the SDF stores two values
  - Weighted sum of signed distances  $D_t(\mathbf{x})$
  - Sum of all weights  $W_t(\mathbf{x})$
- When new range image arrives, update every voxel cell according to

$$D_{t+1}(\mathbf{x}) = D_t(\mathbf{x}) + w_{t+1}(\mathbf{x})d_{t+1}(\mathbf{x})$$
$$W_{t+1}(\mathbf{x}) = W_t(\mathbf{x}) + w_{t+1}(\mathbf{x})$$

# **Weighting Function**

Weight each observation according to its confidence



 Weight can additionally be influenced by other modalities (reflectance values, ...)

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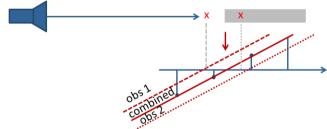
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#### **Two Nice Properties**

Noise cancels out over multiple measurements



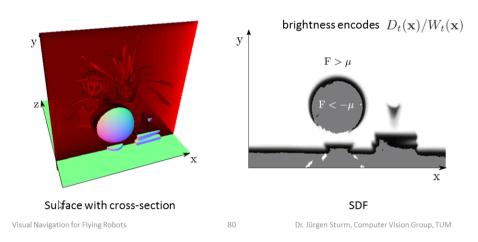
 Zero-crossing can be extracted at sub-voxel accuracy (least squares estimate)

1D Example: 
$$x^* = \frac{\sum D_t(x)x}{\sum W_t(x)x}$$



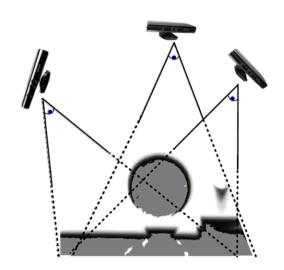
# **SDF Example**

A cross section through a 3D signed distance function of a real scene

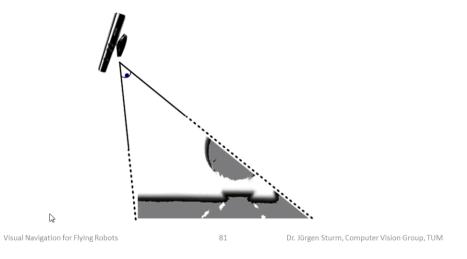




#### **SDF Fusion**



#### **SDF** Fusion





## **Visualizing Signed Distance Fields**

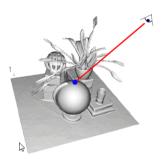
Common approaches to iso surface extraction:

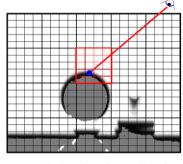
- 1. Ray casting (GPU, fast) For each camera pixel, shoot a ray and search for zero crossing
- 2. Poligonization (CPU, slow) E.g., using the marching cubes algorithm Advantage: outputs triangle mesh



#### **Ray Casting**

- For each camera pixel, shoot a ray and search for the first zero crossing in the SDF
- Value in the SDF can be used to skip along when far from surface





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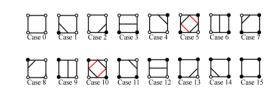
# **Marching Cubes**

#### First in 2D, marching squares:

- Evaluate each cell separately
- Check which edges are inside/outside
- Generate triangles according to lookup table
- Locate vertices using least squares



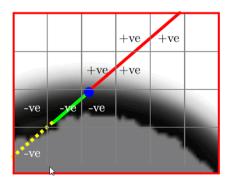


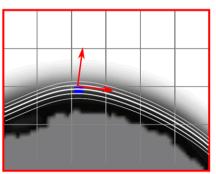




#### **Ray Casting**

- Interpolation reduces artifacts
- Close to surface, gradient represents the surface normal



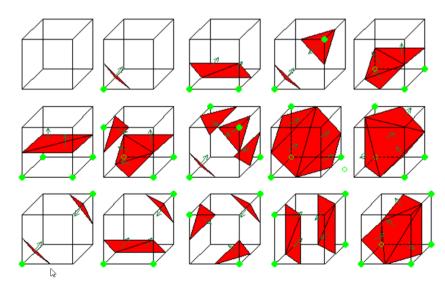


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# **Marching Cubes**



#### **KinectFusion**

[Newcombe et al., 2011]

- Projective ICP with point-to-plane metric
- Truncated signed distance function (TSDF)
- Ray Casting



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#### **KinectFusion**

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[Newcombe et al., 2011]

- Projective ICP with point-to-plane metric
- Truncated signed distance function (TSDF)
- Ray Casting

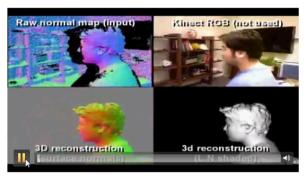




#### **KinectFusion**

[Newcombe et al., 2011]

- Projective ICP with point-to-plane metric
- Truncated signed distance function (TSDF)
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#### **KinectFusion**

[Newcombe et al., 2011]

- Projective ICP with point-to-plane metric
- Truncated signed distance function (TSDF)
- Ray Casting

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#### **KinectFusion**

[Newcombe et al., 2011]

- Projective ICP with point-to-plane metric
- Truncated signed distance function (TSDF)
- Ray Casting





## **Lessons Learned Today**

- How to quickly recognize previously seen places
- How to align point clouds
- How to estimate occupancy maps
- How to reconstruct triangle meshes at subvoxel accuracy

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