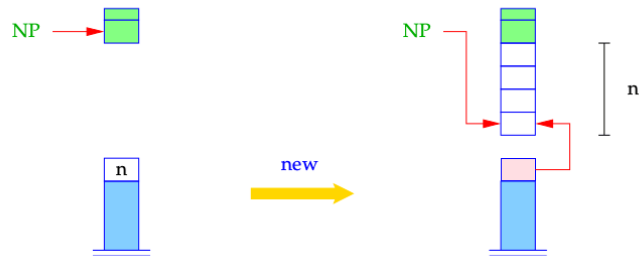


Title: Seidl: Virtual\_Machines (25.04.2016)

Date: Mon Apr 25 10:22:32 CEST 2016

Duration: 90:30 min

Pages: 40



```
if (NP - S[SP] <= EP)
  S[SP] = NULL;
else {
  NP = NP - S[SP];
  S[SP] = NP;
}
```

- NULL is a special pointer constant, identified with the integer constant 0.
- In the case of a collision of stack and heap the NULL-pointer is returned.

What can we do with pointers (pointer values)?

- **set** a pointer to a storage cell,
- **dereference** a pointer, access the value in a storage cell pointed to by a pointer.

There are two ways to set a pointer:

- (1) A call `malloc(e)` reserves a heap area of the size of the value of `e` and returns a pointer to this area:

$$\text{code}_R \text{ malloc}(e) \rho = \text{code}_R e \rho \text{ new}$$

- (2) The application of the address operator `&` to a variable returns a **pointer** to this variable, i.e. its address ( $\hat{=}$  **L-value**). Therefore:

$$\text{code}_R (\&e) \rho = \text{code}_L e \rho$$

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## Dereferencing of Pointers

The application of the operator `*` to the expression  $e$  returns the **contents** of the storage cell, whose address is the R-value of  $e$ :

$$\text{code}_L(*e) \rho = \text{code}_R e \rho$$

**Example** Given the declarations

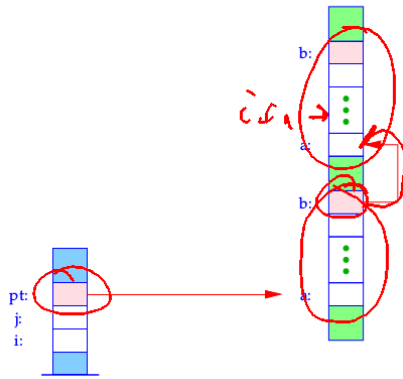
```
struct t { int a[7]; struct t *b; };
int i, j;
struct t *pt;
```

and the expression  $((pt \rightarrow b) \rightarrow a)[i+1]$

Because of  $e \rightarrow a \equiv (*e).a$  holds:

$$\begin{aligned} \text{code}_L(e \rightarrow a) \rho &= \text{code}_R e \rho \\ &\quad \text{loadc}(\rho a) \\ &\quad \text{add} \end{aligned}$$

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```
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Be  $\rho = \{i \mapsto 1, j \mapsto 2, pt \mapsto 3, a \mapsto 0, b \mapsto 7\}$ . Then:

$$\begin{aligned} \text{code}_L((pt \rightarrow b) \rightarrow a)[i+1] \rho &= \text{code}_R((pt \rightarrow b) \rightarrow a) \rho \\ &= \text{code}_R(i+1) \rho \\ &\quad \text{loadc} 1 \\ &\quad \text{mul} \\ &\quad \text{add} \\ &\quad \text{loadc} 1 \\ &\quad \text{mul} \\ &\quad \text{add} \end{aligned}$$

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For arrays, their R-value equals their L-value. Therefore:

$$\begin{aligned} \text{code}_R((pt \rightarrow b) \rightarrow a) \rho &= \text{code}_R(pt \rightarrow b) \rho &= & \text{loada } 3 \\ & \text{loadc } 0 & & \text{loadc } 7 \\ & \text{add} & & \text{add} \\ & & & \text{load} \\ & & & \text{loadc } 0 \\ & & & \text{add} \end{aligned}$$

In total, we obtain the instruction sequence:

loada 3	load	loada 1	loadc 1
loadc 7	loadc 0	loadc 1	mul
add	add	add	add

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$$\text{code}_L(*e) \rho = \text{code}_R e \rho$$

$$\text{code}_L x \rho = \text{loadc } (\rho x)$$

$$\text{code}_R(\&e) \rho = \text{code}_L e \rho$$

$$\text{code}_R e \rho = \text{code}_L e \rho \quad \text{if } e \text{ is an array}$$

$$\begin{aligned} \text{code}_R(e_1 \square e_2) \rho &= \text{code}_R e_1 \rho \\ & \text{code}_R e_2 \rho \\ & \text{op} \end{aligned} \quad \text{op instruction for operator '}\square\text{'}$$

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## 7 Conclusion

We tabulate the cases of the translation of expressions:

$$\begin{aligned} \text{code}_L(e_1[e_2]) \rho &= \text{code}_R e_1 \rho \\ & \text{code}_R e_2 \rho \\ & \text{loadc } |t| \\ & \text{mul} \\ & \text{add} \end{aligned} \quad \text{if } e_1 \text{ has type } t^* \text{ or } t[]$$

$$\begin{aligned} \text{code}_L(e.a) \rho &= \text{code}_L e \rho \\ & \text{loadc } (\rho a) \\ & \text{add} \end{aligned}$$

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$$\text{code}_R q \rho = \text{loadc } q \quad q \text{ constant}$$

$$\begin{aligned} \text{code}_R(e_1 = e_2) \rho &= \text{code}_R e_2 \rho \\ & \text{code}_L e_1 \rho \\ & \text{store} \end{aligned}$$

$$\begin{aligned} \text{code}_R e \rho &= \text{code}_L e \rho \\ & \text{load} \end{aligned} \quad \text{otherwise}$$

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```

code(s1s2) ρ =   loadc 7           loadc 5
                  loadc 2           loadc 17
                  loadc 10 // size of int[10] load
                  mul // scaling      loadc 3
                  add                 loadc 10 // size of int[10]
                  loadc 17           mul // scaling
                  store               add
                  pop // end of s1   store
                                      pop // end of s2

```

65

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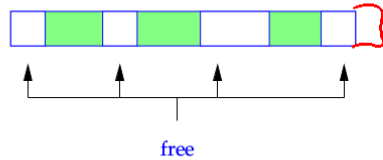
```

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## 8 Freeing Occupied Storage

### Problems

- The freed storage area is still referenced by other pointers (**dangling references**).
- After several deallocations, the storage could look like this (**fragmentation**):



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### Potential Solutions

- Trust the programmer. Manage freed storage in a particular data structure (free list)  $\implies$  `malloc` or `free` may become expensive.
- Do nothing, i.e.:

`code free(e); p` = `codeR e p`  
pop

$\implies$  simple and (in general) efficient.

- Use an **automatic**, potentially "conservative" **Garbage-Collection**, which occasionally collects **certainly** inaccessible heap space.

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## 9 Functions

The definition of a function consists of:

- a **name** by which it can be called;
- a specification of the **formal parameters**;
- a possible **result type**;
- a **block of statements**.

In C, we have:

`codeR f p` = `loadc f` = start address of the code for `f`  
 $\implies$  Function names must be maintained within the address environment!

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### Example

```

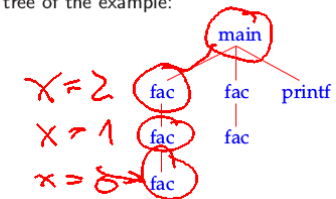
int fac (int x) {
    if (x ≤ 0) return 1;
    else return x * fac(x - 1);
}

main () {
    int n;
    n = fac(2) + fac(1);
    printf ("%d", n);
}

```

At every point of execution, several **instances** (calls) of the same function may be active, i.e., have been started, but not yet completed.

The recursion tree of the example:



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We conclude:

The **formal parameters** and **local variables** of the different calls of the same function (the **instances**) must be kept separate.

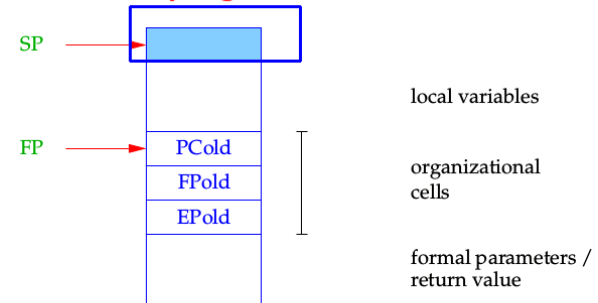
Idea

Allocate a dedicated memory block for each call of a function.

In sequential programming languages, these memory blocks may be maintained on a stack. Therefore, they are also called **stack frames**.

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## 9.1 Memory Organization for Functions



FP  $\hat{=}$  **Frame Pointer**; points to the last **organizational cell** and is used for addressing the formal parameters and local variables.

71

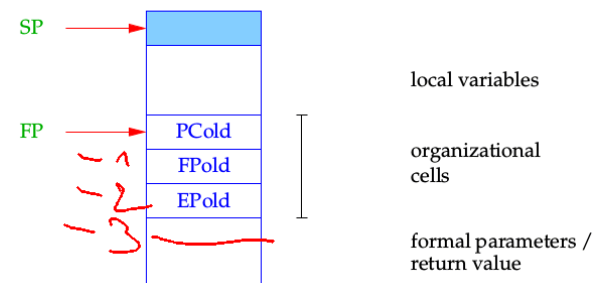
Caveat

- The local variables receive relative addresses  $+1, +2, \dots$
- The formal parameters are placed **below** the organizational cells and therefore have **negative** addresses relative to **FP**.
- This organization is particularly well suited for function calls with **variable** number of arguments as, e.g., for **printf**.
- The memory block of parameters is recycled for storing the return value of the function.

**Simplification:** The return value fits into a single memory cell.

72

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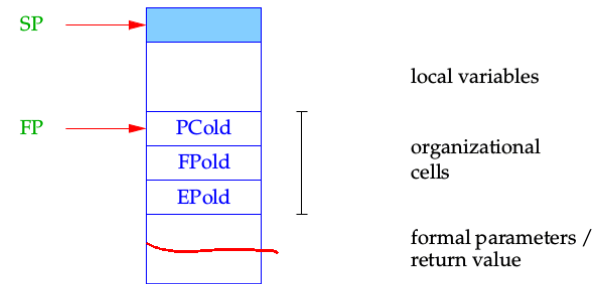
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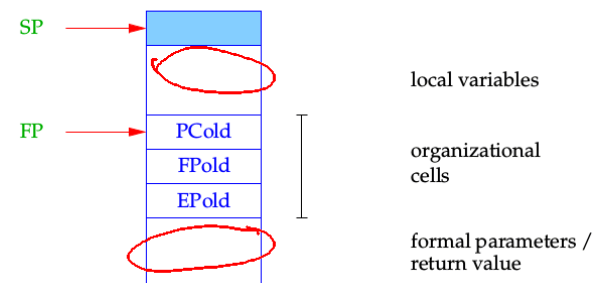
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### Tasks of a Translator for Functions

- Generate code for the body of the function!
- Generate code for calls!

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## 9.2 Determining Address Environments

We distinguish two kinds of variables:

1. **global/extern** that are defined outside of functions;
2. **local/intern/automatic** (including formal parameters) which are defined inside functions.



The address environment  $\rho$  maps names onto pairs  $(tag, a) \in \{G, L\} \times \mathbb{Z}$ .

### Caveat

- In general, there are further refined grades of visibility of variables.
- Different parts of a program may be translated relative to different address environments!

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### Example

```
0 int i;
  struct list {
    int info;
    struct list * next;
  } * l;

1 int ith (struct list * x, int i) {
  if (i ≤ 1) return x → info;
  else return ith (x → next, i - 1);
}

2 main () {
  int k;
  scanf ("%d", &i);
  scanlist (&l);
  printf ("\n\t%d\n", ith (l,i));
}
```

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### Address Environments Occurring in the Program

0 Before the Function Definitions:

$$\begin{aligned} \rho_0 : \quad i &\mapsto (G, 1) \\ & \quad l \mapsto (G, 2) \\ & \quad \dots \end{aligned}$$

1 Inside of ith:

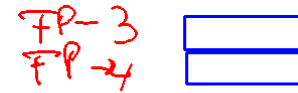
$$\begin{aligned} \rho_1 : \quad i &\mapsto (L, -4) \\ & \quad x \mapsto (L, -3) \\ & \quad \quad l \mapsto (G, 2) \\ & \quad \quad \text{ith} \mapsto (G, \text{ith}) \\ & \quad \quad \dots \end{aligned}$$

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### Caveat

- The actual parameters are evaluated from **right to left !!**
- The first parameter resides directly below the organizational cells.
- For a prototype  $\tau f(\tau_1 x_1, \dots, \tau_k x_k)$  we define:
 
$$x_1 \mapsto (L, -2 - |\tau_1|) \quad x_i \mapsto (L, -2 - |\tau_1| - \dots - |\tau_i|)$$

FP →



77

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2  main () {
    int k;
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    scanlist (&l);
    printf ("\n\t%d\n", ith (l,i));
}
```

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2 Inside of main:

```
ρ2 :      i  ↦ (G, 1)
          l  ↦ (G, 2)
          k  ↦ (L, 1)
          ith ↦ (G, _ith)
          main ↦ (G, _main)
          ...
```

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## 9.3 Calling/Entering and Exiting/Leaving Functions

Assume that  $f$  is the current function, i.e., the **caller**, and  $f$  calls the function  $g$ , i.e., the **callee**.

The code for the call must be distributed between the caller and the callee.

The distribution can only be such that the code depending on information of the caller must be generated for the caller and likewise for the callee.

### Caveat

The space requirements of the actual parameters is only known to the caller ...

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Actions when entering  $g$ :

1. Evaluating the actual parameters
  2. Saving of FP, EP
  3. Determining the start address of  $g$
  4. Setting of the new FP
  5. Saving PC and  
Jump to the beginning of  $g$
  6. Setting of new EP
  7. Allocating of local variables
- } mark } are part of  $f$
- } call }
- } enter } are part of  $g$
- } alloc }