

Script generated by TTT

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Pages: 36

Otherwise, we could implement the run-time function `check()` as follows:

```
bool check (ref u, ref v) {
  if (u == v) return false;
  if (H[v] == (S, f/n)) {
    for (int i=1; i<=n; i++)
      if (!check(u, deref (H[v+i])))
        return false;
    return true;
  }
}
```

$$X = t$$

- The run-time function `trail()` records the a potential new binding.
- The run-time function `backtrack()` initiates backtracking.
- The auxiliary function `check()` performs the occur-check: it tests whether a variable (the first argument) occurs inside a term (the second argument).
- Often, this check is skipped, i.e.,

```
bool check (ref u, ref v) { return true;}
```

Discussion:

$$X = a$$

- The translation of an equation $X = t$ is very simple :-)
- Often the constructed cells immediately become garbage :-)

Idea 2:

- Push a reference to the run-time binding of the left-hand side onto the stack.
- Avoid to construct sub-terms of t whenever possible !
- Translate each node of t into an instruction which performs the unification with this node !!

Discussion:

- The translation of an equation $\tilde{X} = t$ is very simple :-)
- Often the constructed cells immediately become *garbage* :-)

Idea 2:

- Push a reference to the run-time binding of the left-hand side onto the stack.
- Avoid to construct sub-terms of t whenever possible !
- Translate each node of t into an instruction which performs the unification with this node !!

$$\text{code}_G(\tilde{X} = t) \rho = \text{put } \tilde{X} \rho$$

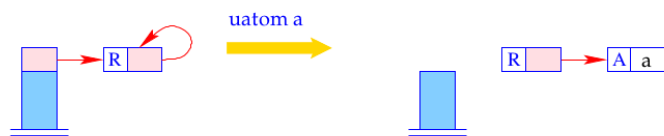
$$\text{code}_U t \rho \quad \leftarrow$$

Let us first consider the unification code for atoms and variables only:

```

code_U a ρ = uatom a
code_U X ρ = uvar (ρ X)
code_U _ ρ = pop
code_U  $\tilde{X}$  ρ = uref (ρ X)
... // to be continued :-)
```

The instruction `uatom a` implements the unification with the atom `a`:



```

v = S[SP]; SP--;
switch (H[v]) {
case (A, a): break;
case (R, _): H[v] = (R, new (A, a));
             trail (v); break;
default:    backtrack();
}
```

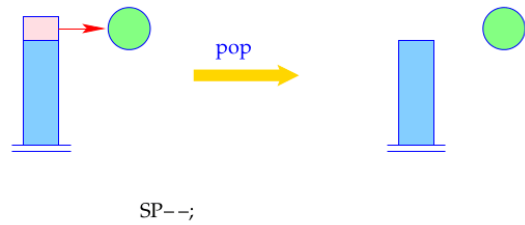
- The run-time function `trail()` records the a potential new binding.
- The run-time function `backtrack()` initiates *backtracking*.

The instruction `uvar i` implements the unification with an un-initialized variable:



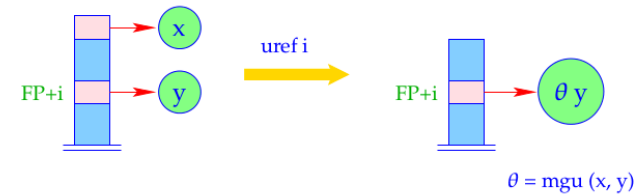
```
S[FP+i] = S[SP]; SP--;
```

The instruction `pop` implements the unification with an anonymous variable. It always succeeds :-)



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The instruction `uref i` implements the unification with an initialized variable:



unify (S[SP], deref (S[FP+i]));
SP--;

It is only here that the run-time function `unify()` is called :-)

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- The unification code performs a **pre-order** traversal over t .
- In case, execution hits at an unbound variable, we **switch** from checking to building :-)

```
codeU f(t1, ..., tn) ρ =   ustruct f/n A           // test
                             son 1
                             codeU t1 ρ
                             ...
                             son n
                             codeU tn ρ
                             up B
                             A : check ivars(f(t1, ..., tn)) ρ // occur-check
                             codeA f(t1, ..., tn) ρ           // building !!
                             bind                               // creation of bindings
                             B : ...
```

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                             B : ...
```

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The Building Block:

Before constructing the new (sub-) term t' for the binding, we must exclude that it contains the variable X' on top of the stack !!!

This is the case iff **the binding** of no variable inside t' contains (a reference to) X' .

⇒ $ivars(t')$ returns the set of **already initialized** variables of t .

⇒ The macro `check` $\{Y_1, \dots, Y_d\} \rho$ generates the necessary tests on the variables Y_1, \dots, Y_d :

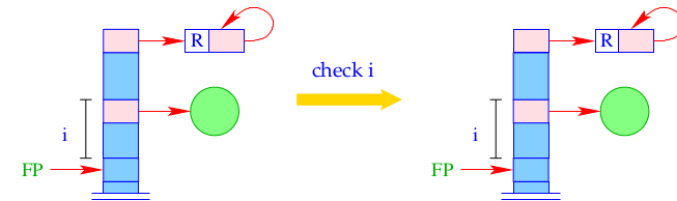
```

check {Y1, ..., Yd} ρ =  check (ρ Y1)
                          check (ρ Y2)
                          ...
                          check (ρ Yd)
    
```

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The instruction `check i` checks whether the (unbound) variable on top of the stack occurs inside the term bound to variable i .

If so, unification fails and **backtracking** is caused:



```

if (!check (S[SP], deref S[FP+i]))
  backtrack();
    
```

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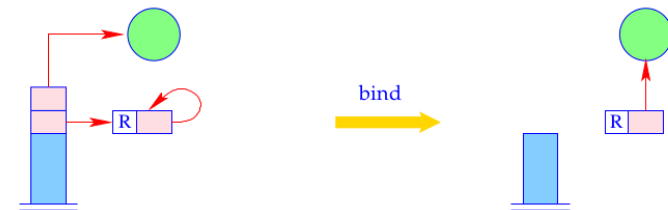
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A :  check ivars(f(t1, ..., tn)) ρ  // occur-check
     codeA f(t1, ..., tn) ρ      // building !!
     bind                               // creation of bindings
B :  ...
    
```

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The instruction `bind` terminates the building block. It binds the (unbound) variable to the constructed term:



```

H[S[SP-1]] = (R, S[SP]);
trail (S[SP-1]);
SP = SP - 2;
    
```

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- In case, execution hits at an unbound variable, we **switch** from checking to building :-)

```

codeU f(t1, ..., tn) ρ =   ustruct f/n A           // test
                             son 1                 // recursive descent
                             codeU t1 ρ
                             ...
                             son n                 // recursive descent
                             codeU tn ρ
                             up B                   // ascent to father
A : check ivars(f(t1, ..., tn)) ρ // occur-check
    codeA f(t1, ..., tn) ρ // building !!
    bind // creation of bindings
B : ...

```

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The Pre-Order Traversal:

- First, we **test** whether the topmost reference is an unbound variable. If so, we jump to the building block.
- Then we compare the root node with the constructor f/n .
- Then we **recursively descend** to the children.
- Then we **pop** the stack and proceed behind the unification code:

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Once again the unification code for constructed terms:

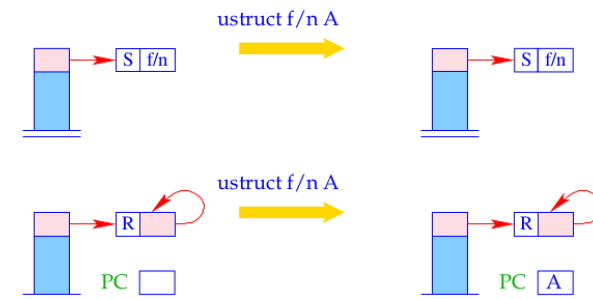
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codeU f(t1, ..., tn) ρ =   ustruct f/n A           // test
                             son 1                 // recursive descent
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A : check ivars(f(t1, ..., tn)) ρ // occur-check
    codeA f(t1, ..., tn) ρ // building !!
    bind // creation of bindings
B : ...

```

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The instruction **ustruct i** implements the test of the root node of a structure:



```

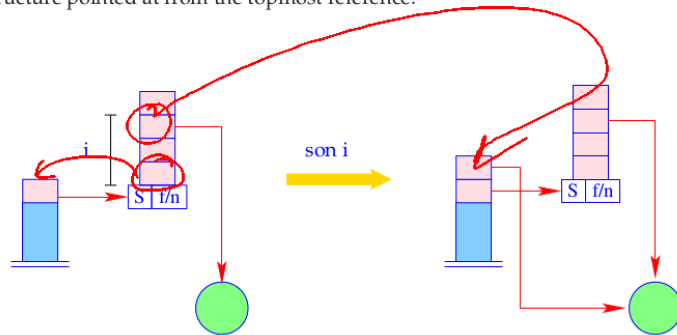
switch (H[S[SP]]) {
case (S, f/n):  break;
case (R, _):   PC = A; break;
default:       backtrack();
}

```

... the argument reference is **not yet popped** :-)

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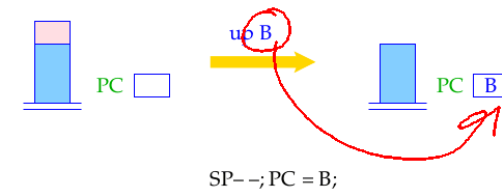
The instruction `son i` pushes the (reference to the) i -th sub-term from the structure pointed at from the topmost reference:



$S[SP+1] = \text{deref}(H[S[SP]+i]); SP++;$

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It is the instruction `up B` which finally pops the reference to the structure:



The continuation address `B` is the next address after the `build`-section.

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Example:

For our example term $f(g(\bar{X}, Y), a, Z)$ and $\rho = \{X \mapsto 1, Y \mapsto 2, Z \mapsto 3\}$ we obtain:

ustruct f/3 A_1	up B_2	B_2 :	son 2	putvar 2
son 1			uatom a	putstruct g/2
ustruct g/2 A_2	A_2 :	check 1	son 3	putatom a
son 1	putref 1	uvar 3	putvar 3	
uref 1	putvar 2	up B_1	putstruct f/3	
son 2	putstruct g/2	A_1 :	check 1	bind
uvar 2	bind	putref 1	B_1 :	...

Code size can grow quite considerably — for `deep` terms. In practice, though, deep terms are “rare” :-)

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son 1	putref 1	uvar 3	putvar 3	
uref 1	putvar 2	up B_1	putstruct f/3	
son 2	putstruct g/2	A_1 :	check 1	bind
uvar 2	bind	putref 1	B_1 :	...

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32 Clauses

Clausal code must

- **allocate** stack space for locals;
- **evaluate** the body;
- **free** the stack frame (whenever possible :-)

Let r denote the clause: $p(X_1, \dots, X_k) \leftarrow g_1, \dots, g_n.$

Let $\{X_1, \dots, X_m\}$ denote the set of locals of r and ρ the address environment:

$$\rho X_i = i$$

Remark: The first k locals are always the **formals** :-)

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Then we translate:

```
codeC r = pushenv m      // allocates space for locals
          codeC g1 ρ
          ...
          codeC gn ρ
          popenv
```

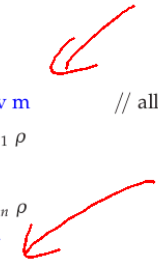
The instruction **popenv** restores **FP** and **PC** and **tries to pop** the current stack frame.

It should succeed whenever program execution will never return to this stack frame :-)

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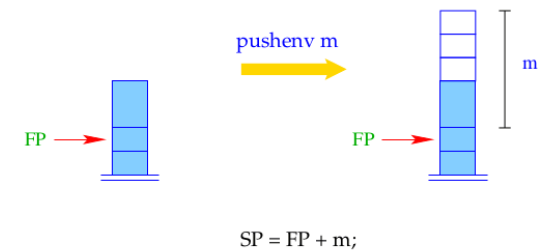


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The instruction **pushenv m** sets the stack pointer:



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Example:

Consider the clause r :

$$a(X, Y) \leftarrow f(\bar{X}, X_1), a(\bar{X}_1, \bar{Y})$$

Then $\text{code}_C r$ yields:

```
pushenv 3      mark A      A: mark B      B: popenv
                putref 1
                putvar 3
                call f/2
                putref 3
                putref 2
                call a/2
```

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33 Predicates

A predicate q/k is defined through a sequence of clauses $rr \equiv r_1 \dots r_f$.

The translation of q/k provides the translations of the individual clauses r_i .

In particular, we have for $f = 1$:

$$\text{code}_P rr = \text{code}_C r_1$$

If q/k is defined through several clauses, the first alternative must be tried.

On failure, the next alternative must be tried

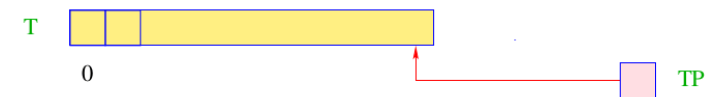
\implies backtracking :-)

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33.1 Backtracking

- Whenever unification fails, we call the run-time function `backtrack()`.
- The goal is to **roll back** the whole computation to the (dynamically :-) latest goal where another clause can be chosen \implies the last **backtrack point**.
- In order to undo intermediate variable bindings, we always have recorded new bindings with the run-time function `trail()`.
- The run-time function `trail()` stores variables in the data-structure **trail**:

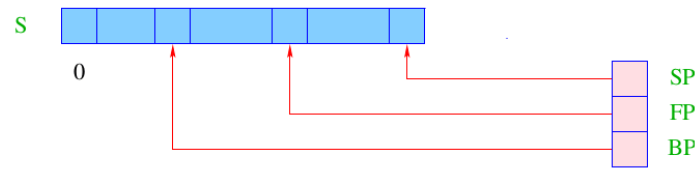
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TP \implies Trail Pointer
points to the topmost occupied Trail cell

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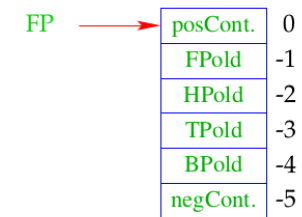
The current stack frame where backtracking should return to is pointed at by the extra register **BP**:



A **backtrack point** is stack frame to which program execution possibly returns.

- We need the code address for trying the **next** alternative (**negative continuation address**);
- We save the old values of the registers **HP**, **TP** and **BP**.
- **Note:** The **new BP** will receive the value of the current **FP** :-)

For this purpose, we use the corresponding four organizational cells:



For more comprehensible notation, we thus introduce the macros:

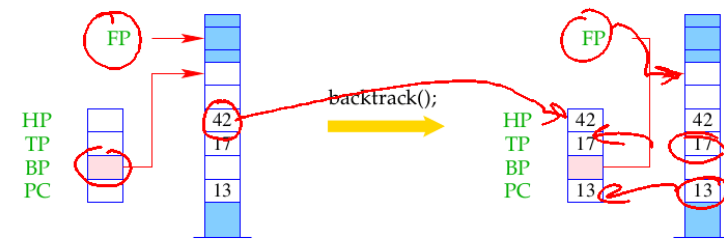
- `posCont` \equiv `S[FP]`
- `FPold` \equiv `S[FP - 1]`
- `HPold` \equiv `S[FP - 2]`
- `TPold` \equiv `S[FP - 3]`
- `BPold` \equiv `S[FP - 4]`
- `negCont` \equiv `S[FP - 5]`

for the corresponding addresses.

Remark:

- Occurrence on the **left** \equiv saving the register
- Occurrence on the **right** \equiv restoring the register

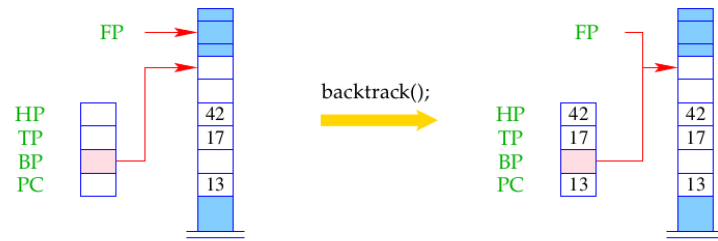
Calling the run-time function `void backtrack()` yields:



```
void backtrack() {
    FP = BP; HP = HPold;
    reset (TPold, TP);
    TP = TPold; PC = negCont;
}
```

where the run-time function `reset()` undoes the bindings of variables established **since** the backtrack point.

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void backtrack() {  
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