Script generated by TTT

Title: Seidl: Virtual_Machines (07.05.2013)

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Accessing Global Variables



- The bindings of global variables of an expression or a function are kept in a vector in the heap (Global Vector).
- They are addressed consecutively starting with 0.
- When an F-object or a C-object are constructed, the Global Vector for the function or the expression is determined and a reference to it is stored in the gp-component of the object.
- During the evaluation of an expression, the (new) register GP (Global Pointer) points to the actual Global Vector.
- In constrast, local variables should be administered on the stack ...

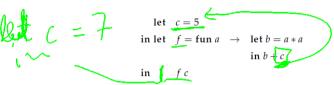
── General form of the address environment:

$$\rho: Vars \rightarrow \{L,G\} \times \mathbb{Z}$$

14 Accessing Variables

We must distinguish between local and global variables.

Example: Regard the function f:



The function f uses the global variable c and the local variables a (as formal parameter) and b (introduced by the inner let).

The binding of a global variable is determined, when the function is constructed (static scoping!), and later only looked up.

115

Accessing Local Variables

Local variables are administered on the stack, in stack frames.

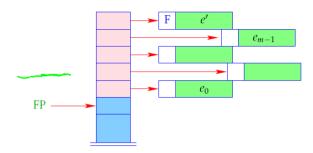
Let $e \equiv e' \ e_0 \ \dots \ e_{m-1}$ be the application of a function e' to arguments e_0, \dots, e_{m-1} .

Warning:

The arity of e' does not need to be m:-)

- *f* may therefore receive less than *n* arguments (under supply);
- f may also receive more than n arguments, if t is a functional type (over supply).

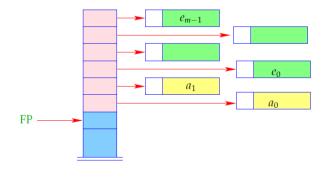
Possible stack organisations:



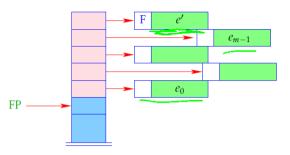
- + Addressing of the arguments can be done relative to FP
- The local variables of e' cannot be addressed relative to FP.
- If e' is an n-ary function with n < m, i.e., we have an over-supplied function application, the remaining m n arguments will have to be shifted.

118

— If e' evaluates to a function, which has already been partially applied to the parameters a_0, \ldots, a_{k-1} , these have to be sneaked in underneath e_0 :



Possible stack organisations:

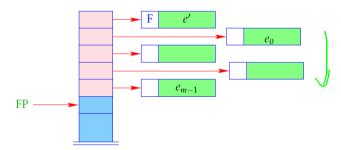


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118

Alternative:

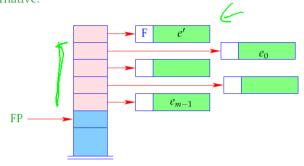
l 20-2: em-1



+ The further arguments a_0, \ldots, a_{k-1} and the local variables can be allocated above the arguments.

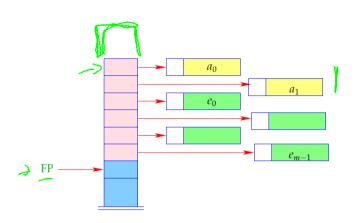
119

Alternative:



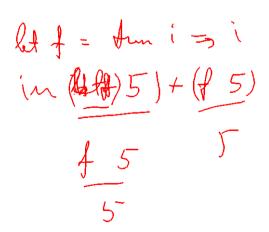
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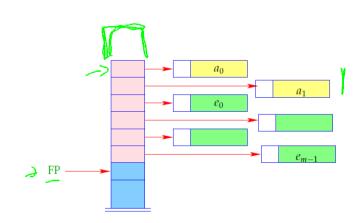
120



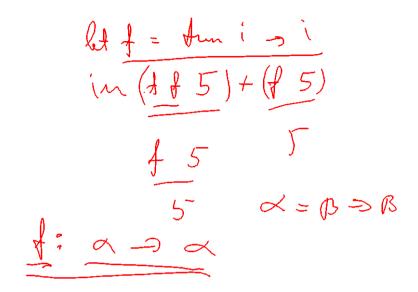
 Addressing of arguments and local variables relative to FP is no more possible. (Remember: *m* is unknown when the function definition is translated.)

121



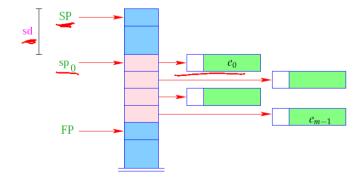


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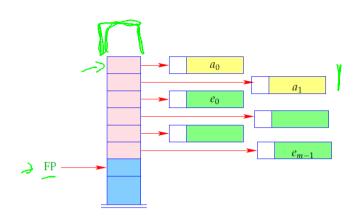


Way out:

- We address both, arguments and local variables, relative to the stack pointer
 SP !!!
- However, the stack pointer changes during program execution...



122



 Addressing of arguments and local variables relative to FP is no more possible. (Remember: m is unknown when the function definition is translated.)

121

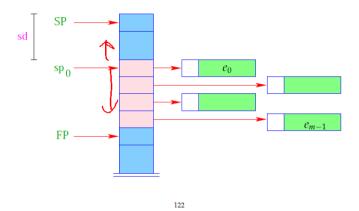
- ullet The difference between the current value of SP and its value sp_0 at the entry of the function body is called the stack distance, sd .
- Fortunately, this stack distance can be determined at compile time for each program point, by simulating the movement of the SP.
- The formal parameters x_0, x_1, x_2, \dots successively receive the non-positive relative addresses $0, -1, -2, \dots$, i.e., $\rho x_i = (L, -i)$.
- The absolute address of the *i*-th formal parameter consequently is

$$sp_0 - i = (SP - sd) - i$$

• The local let-variables y_1, y_2, y_3, \dots will be successively pushed onto the stack:

Way out:

- However, the stack pointer changes during program execution...



- The difference between the current value of SP and its value sp₀ at the entry of the function body is called the stack distance, sd.
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$$\mathrm{sp}_0 - i = (\mathrm{SP} - \mathrm{sd}) - i$$

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123

• The y_i have positive relative addresses 1, 2, 3, . . ., that is: $\rho y_i = (L, i)$.

• The absolute address of y_i is then $sp_0 + i = (SP - sd) + i$

With CBN, we generate for the access to a variable:

$$code_V \underbrace{x \rho}_{sd} sd = getvar x \rho sd$$

$$eval$$

The instruction eval checks, whether the value has already been computed or whether its evaluation has to yet to be done (will be treated later :-)

With CBV, we can just delete eval from the above code schema.

The (compile-time) macro getvar is defined by:

125

The access to local variables:



$$S[SP+1] = S[SP - n]; SP++;$$

126

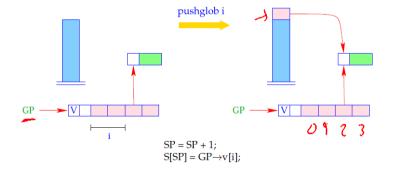
Correctness argument:

Let sp and sd be the values of the stack pointer resp. stack distance before the execution of the instruction. The value of the local variable with address i is loaded from S[a] with

$$a = \operatorname{sp} - (\operatorname{sd} - i) = (\operatorname{sp} - \operatorname{sd}) + i = \operatorname{sp}_0 + i$$
 ... exactly as it should be :-)

127

The access to global variables is much simpler:



Example:

Regard
$$e\equiv (b+c)$$
 for $\rho=\{b\mapsto (L,1),c\mapsto (G,0)\}$ and ${\rm sd}=1.$ With CBN, we obtain:

15 let-Expressions

As a warm-up let us first consider the treatment of local variables :-)

Let $e \equiv \text{let } y_1 = e_1 \text{ in } \dots \text{let } e_n \text{ in } e_0$ be a nested let-expression.

The translation of e must deliver an instruction sequence that

- allocates local variables y_1, \ldots, y_n ;
- in the case of

CBV: evaluates e_1, \ldots, e_n and binds the y_i to their values;

CBN: constructs closures for the e_1, \ldots, e_n and binds the y_i to them;

• evaluates the expression e_0 and returns its value.

Here, we consider the non-recursive case only, i.e. where y_j only depends on y_1, \ldots, y_{j-1} . We obtain for CBN:

130

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```
\operatorname{code}_{V} \times \rho \operatorname{sd} = \operatorname{getvar} x \rho \operatorname{sd}
\operatorname{eval}
```

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With CBV, we can just delete eval from the above code schema.

The (compile-time) macro getvar is defined by:

```
\begin{array}{lll} \operatorname{getvar} x \ \rho \operatorname{sd} &=& \operatorname{let} \left( t, i \right) = \rho \ x \operatorname{in} \\ & \operatorname{match} t \operatorname{with} \\ & L \to \operatorname{pushloc} \left( \operatorname{sd} - i \right) \\ & \mid G \to \operatorname{pushglob} i \end{array}
```

125

15 let-Expressions

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```
\begin{array}{rcl} \operatorname{code}_{V} e \, \rho \operatorname{sd} & = & \operatorname{code}_{\mathbb{C}} e_{1} \, \rho \operatorname{sd} \\ & & \operatorname{code}_{\mathbb{C}} e_{2} \, \rho_{1} \, (\operatorname{sd} + 1) \\ & & & \cdots \\ & & & \operatorname{code}_{\mathbb{C}} e_{n} \, \rho_{n-1} \, (\operatorname{sd} + n - 1) \\ & & & & \operatorname{code}_{\mathbb{C}} e_{0} \, \rho_{n} \, (\operatorname{sd} + n) \\ & & & & & \operatorname{slide} n \end{array}
```

where $\rho_j = \rho \oplus \{y_i \mapsto (L, \operatorname{sd} + i) \mid i = 1, \dots, j\}.$

In the case of CBV, we use $code_V$ for the expressions e_1, \ldots, e_n .

Warning!

All the e_i must be associated with the same binding for the global variables!

131

```
Si = {a -> (L,2)}
```

Example:

Consider the expression

 $e \equiv \text{let } a = 19 \text{ in let } b = a * a \text{ in } a + b$

for $\rho = \emptyset$ and sd = 0. We obtain (for CBV):

132

```
\begin{array}{rcl} \operatorname{code}_{V} e \ \rho \ \operatorname{sd} & = & \operatorname{code}_{C} e_{1} \ \rho \ \operatorname{sd} \\ & & \operatorname{code}_{C} e_{2} \ \rho_{1} \ (\operatorname{sd} + 1) \\ & & \cdots \\ & & & \operatorname{code}_{C} e_{n} \ \rho_{n-1} \ (\operatorname{sd} + n - 1) \\ & & & \operatorname{code}_{V} e_{0} \ \rho_{n} \ (\operatorname{sd} + n) \\ & & & & \operatorname{slide} n \end{array}
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 $g_0 = \left\{ a \rightarrow (\ell, 1) \right\}$ guton a $p_0 = 2 = 2$

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1 - 2 -) a de

pushloc 1

getbasic

add

- loadc 19
 3
 getbasic
 3

 mkbasic
 3
 mul
 4

 pushloc 0
 2
 mkbasic
 4
- 2 getbasic 2 pushloc 1 3 mkbasic 2 pushloc 1 3 getbasic 3 slide 2

132

The instruction slide k deallocates again the space for the locals:

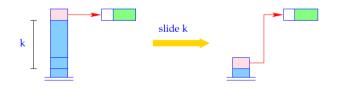


$$S[SP-k] = S[SP];$$

 $SP = SP - k;$

133

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$$e \equiv \text{let } a = 19 \text{ in let } b = a * a \text{ in } a + b$$

for $\rho = \emptyset$ and sd = 0. We obtain (for CBV):

- 0 loadc 19 3 getbasic
 - 3 mul
- 3 pushloc 14 getbasic

1 pushloc 0

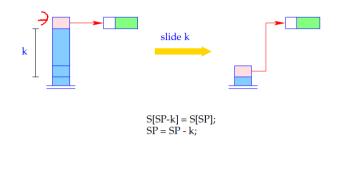
mkbasic

- 2 mkbasic
- 4 add

- 2 getbasic
- 2 pushloc 1
- 3 mkbasic

- 2 pushloc 1
- 3
 - getbasic
- slide 2

The instruction slide k deallocates again the space for the locals:



133

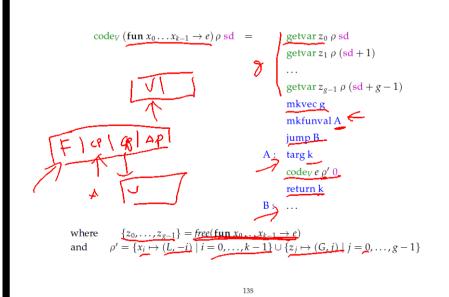
16 Function Definitions

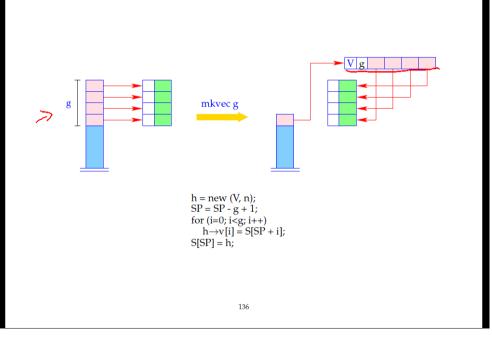
The definition of a function f requires code that allocates a functional value for f in the heap. This happens in the following steps:

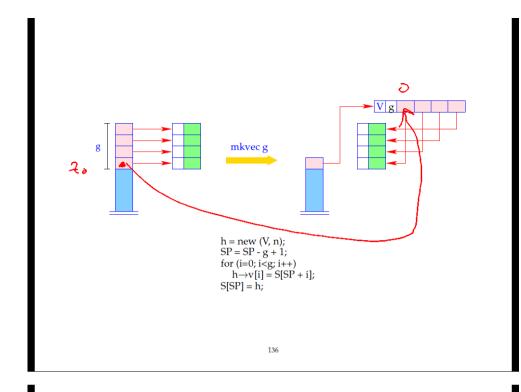
- Creation of a Global Vector with the binding of the free variables;
- Creation of an (initially empty) argument vector;
- Creation of an F-Object, containing references to theses vectors and the start address of the code for the body;

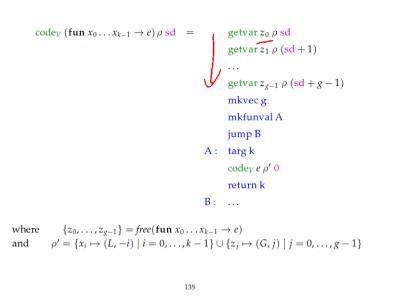
Separately, code for the body has to be generated.

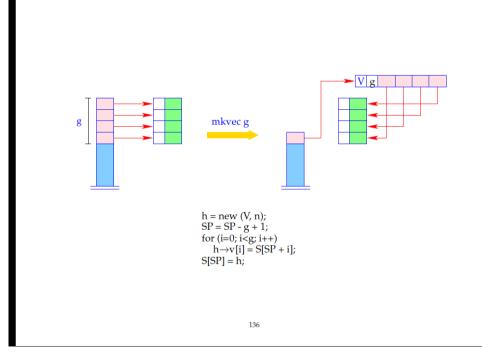
Thus:

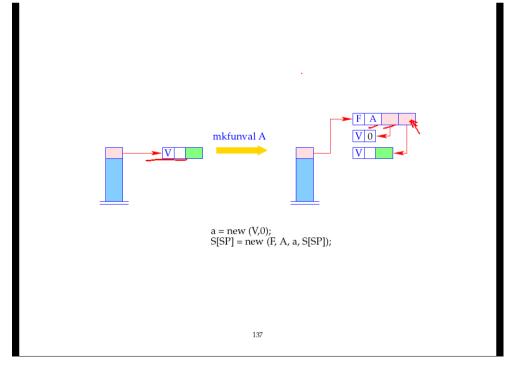












Example:

Regard
$$f \equiv \text{fun } b \rightarrow a + b$$
 for $\rho = \{a \mapsto (L, 1)\}$ and $sd = 1$. $code_V f \rho 1$ produces:

```
0 pushglob 0
                                                   getbasic
       pushloc 0
       mkvec 1
                        1 eval
                                                   add
2
       mkfunval A
                        1 getbasic
                                                  mkbasic
2
       jump B
                        1 pushloc 1
                                                  return 1
0 A: targ 1
                                            2 B: ...
                        2 eval
```

The secrets around targ k and return k will be revealed later:-)

138

→ FIAITA

Regard $f \equiv \text{fun } b \rightarrow a + b$ for $\rho = \{a \mapsto (L, 1)\}$ and sd = 1.

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138

 1
 pushloc 0
 0
 pushglob 0
 2
 getbasic

 2
 mkvec 1
 1
 eval
 2
 add

 2
 mkfunval A
 1
 getbasic
 1
 mkbasic

 2
 jump B
 1
 pushloc 1
 1
 return 1

 0
 A:
 targ 1
 2
 eval
 2
 B:
 ...

The secrets around targ k and return k will be revealed later :-)

17 Function Application

Function applications correspond to function calls in \mathbb{C} . The necessary actions for the evaluation of $e'e_0\ldots e_{m-1}$ are:

- Allocation of a stack frame;

CBV: Evaluation of the actual parameters;
CBN: Allocation of closures for the actual parameters;

- Evaluation of the expression *e'* to an F-object;
- Application of the function.

Thus for CBN:

Example:

```
 \begin{array}{rcl} \operatorname{code}_{V}\left(e'\,e_{0}\,\ldots\,e_{m-1}\right)\rho\,\operatorname{sd} &=& \underset{\quad \operatorname{code}_{C}\,e_{m-1}\,\rho\,\left(\operatorname{sd}+3\right)}{\operatorname{code}_{C}\,e_{m-1}\,\rho\,\left(\operatorname{sd}+4\right)} \\ && \underset{\quad \ldots}{\operatorname{code}_{C}\,e_{m-2}\,\rho\,\left(\operatorname{sd}+4\right)} \\ && \underset{\quad \ldots}{\ldots} \\ && \underset{\quad \operatorname{code}_{V}\,e'\,\rho\,\left(\operatorname{sd}+m+2\right)}{\operatorname{code}_{V}\,e'\,\rho\,\left(\operatorname{sd}+m+3\right)} & \text{// Evaluation of } e' \\ && \underset{\quad \  \  }{\operatorname{apply}} && \underset{\quad \  \  }{\text{// corresponds to call}} \\ && A: \ldots \end{array}
```

To implement CBV, we use $code_V$ instead of $code_C$ for the arguments e_i .

Example: For
$$(f 42)$$
, $\rho = \{ \underline{f} \mapsto (L, \underline{2}) \}$ and $\underline{sd} = \underline{2}$, we obtain with CBV:

- 2 mark A
- 6 mkbasic
- 7 apply
- 5 loadc 42 6 pushloc 4 3 A: ...
 - 6-2

140

A Slightly Larger Example:

let
$$a = 17$$
 in let $f = \text{fun } b \rightarrow a + b$ in f 42

For CBV and sd = 0 we obtain:

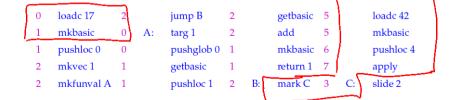
```
loadc 17
                     jump B
                                         getbasic 5
                                                           loadc 42
           0 A:
                    targ 1
                                         add
                                                           mkbasic
mkbasic
pushloc 0
                     pushglob 0 1
                                         mkbasic 6
                                                           pushloc 4
                     getbasic
mkvec 1
                                         return 1 7
                                                           apply
                     pushloc 1 2
                                                          slide 2
mkfunval A 1
                                         mark C 3
```

141

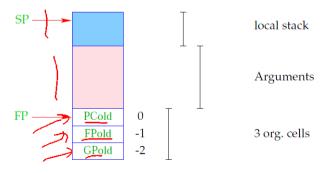
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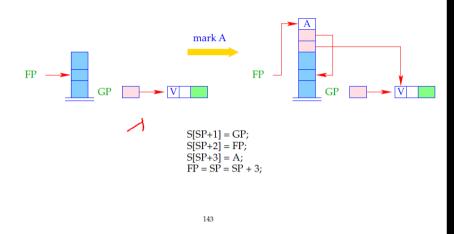


For the implementation of the new instruction, we must fix the organization of a stack frame:

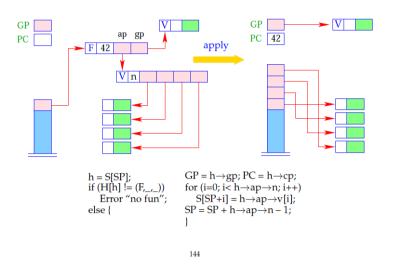


141

Different from the CMa, the instruction $\ \ \, mark\ A \ \ \, already$ saves the return address:

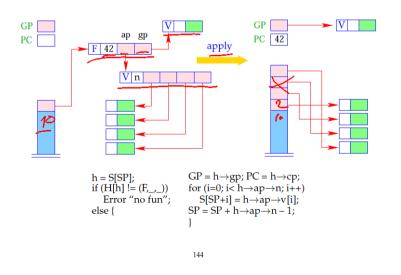


The instruction apply unpacks the F-object, a reference to which (hopefully) resides on top of the stack, and continues execution at the address given there:





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Warning:

- The last element of the argument vector is the last to be put onto the stack.
 This must be the first argument reference.
- This should be kept in mind, when we treat the packing of arguments of an under-supplied function application into an F-object !!!

18 Over– and Undersupply of Arguments

The first instruction to be executed when entering a function body, i.e., after an apply $is \quad targ \ k \ .$

This instruction checks whether there are enough arguments to evaluate the body.

Only if this is the case, the execution of the code for the body is started.

Otherwise, i.e. in the case of under-supply, a new F-object is returned.

The test for number of arguments uses: SP – FP