

Script generated by TTT

Title: Petter: Compilerbau (22.06.2015)

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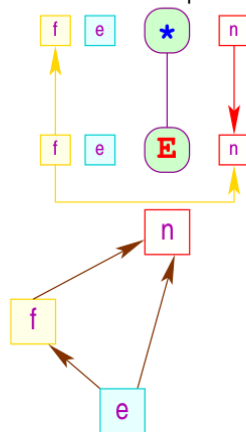
From Dependencies to Evaluation Strategies

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- let the **user** define the evaluation order
- automatic** strategy based on the dependencies:
 - use local dependencies to determine which attributes to compute
 - suppose we require $n[1]$
 - computing $n[1]$ requires $f[1]$
 - $f[1]$ depends on an attribute in the child, so descend
 - compute attributes in **passes**
 - compute a dependency graph between attributes (no go if cyclic)
 - traverse AST once for each attribute; here three times, once for e, f, n
 - compute one attribute in each pass

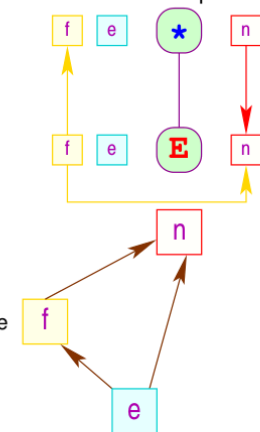


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 - compute attributes in passes
 - compute a dependency graph between attributes (no go if cyclic)
 - traverse AST once for each attribute; here three times, once for e, f, n
 - compute one attribute in each pass
- consider a **fixed** strategy and only allow an attribute system that can be evaluated using this strategy



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Linear Order from Dependency Partial Order

Possible *automatic* strategies:

- 1 demand-driven evaluation
 - start with the evaluation of any required attribute
 - if the equation for this attribute relies on as-of-yet unevaluated attributes, compute these recursively
 - \leadsto visits the nodes of the syntax tree on demand
 - (following a dependency on the parent requires a pointer to the parent)

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 - organize the evaluation of the tree in passes
 - for each pass, pre-compute a strategy to *visit* the nodes together with a *local strategy* for evaluation within each node type

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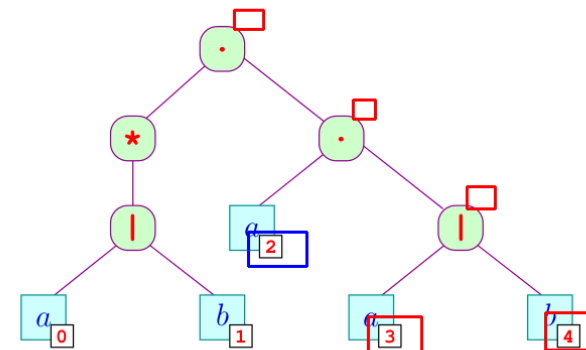
consider example for *demand-driven* evaluation

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Example: Demand-Driven Evaluation

Compute *next* at leaves a_2, a_3 and b_4 in the expression $(a|b)^*a(a|b)$:

$$\begin{aligned} | & : \begin{aligned} \text{next}[1] & := \text{next}[0] \\ \text{next}[2] & := \text{next}[0] \end{aligned} \\ \square & : \begin{aligned} \text{next}[1] & := \text{first}[2] \cup (\text{empty}[2] ? \text{next}[0] : \emptyset) \\ \text{next}[2] & := \text{next}[0] \end{aligned} \end{aligned}$$

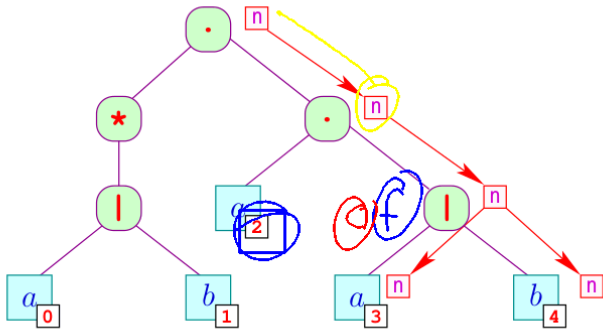


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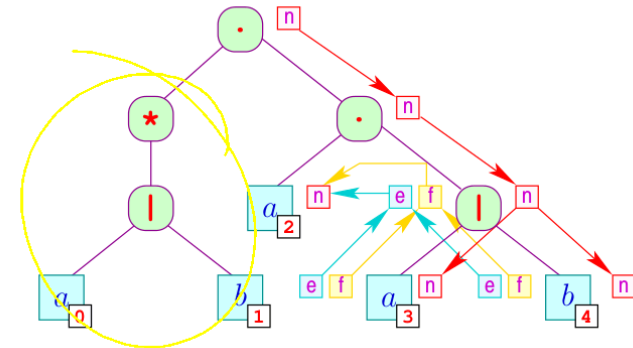


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Demand-Driven Evaluation

Observations

- *only required* attributes are evaluated
- the evaluation sequence depends – in general – on the actual syntax tree
- the algorithm must track which attributes it has already evaluated
- the algorithm may visit nodes more often than necessary
- each node must contain a pointer to its parent
- the algorithm is *not local*

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approach only beneficial in principle:

- evaluation strategy is dynamic: difficult to debug
- computation of all attributes is often cheaper
- usually all attributes in all nodes are required

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Evaluation in Passes

Idea: traverse the syntax tree several times; each time, evaluate all those equations $a[i_a] = f(b[i_b], \dots, z[i_z])$ whose arguments $b[i_b], \dots, z[i_z]$ are known

For a **strongly acyclic attribute system**:

- the local dependencies in D_i of the i th production $N \rightarrow X_1 \dots X_n$ together the global dependencies $\mathcal{R}(X_i)$ for each X_i define a sequence in which attributes can be evaluated
- determine a sequence in which the children are visited so that as many attributes as possible are evaluated
- in each pass at least one new attribute is evaluated
- requires at most n passes for evaluating n attributes
- since a traversal strategy exists for evaluating one attribute, it might be possible to find a strategy to evaluate more attributes \rightsquigarrow optimization problem
- note:** evaluating attribute set $\{a[0], \dots, z[0]\}$ for rule $N \rightarrow \dots N \dots$ may evaluate a different attribute set of its children \rightsquigarrow up to $2^k - 1$ evaluation functions for N

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... in the example:

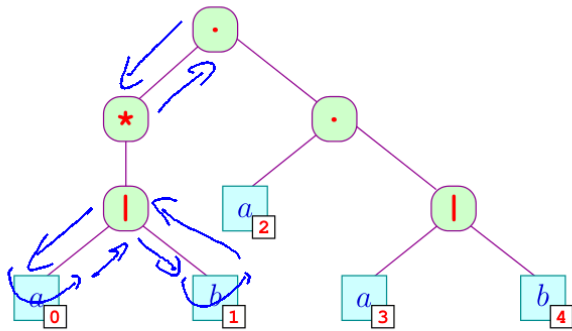
- empty and first can be computed together
- next must be computed in a separate pass

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Implementing State

Problem: In many cases some sort of state is required.

Example: numbering the leafs of a syntax tree



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Implementing Numbering of Leafs

Idea:

- use helper attributes **pre** and **post**
- in **pre** we pass the value of the last leaf down (inherited attribute)
- in **post** we pass the value of the last leaf up (synthetic attribute)

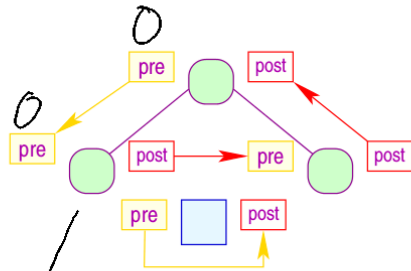
root: $pre[0] := 0$
 $pre[1] := pre[0]$
 $post[0] := post[1]$

node: $pre[1] := pre[0]$
 $pre[2] := post[1]$
 $post[0] := post[2]$

leaf: $post[0] := pre[0] + 1$

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The Local Attribute Dependencies



- the attribute system is apparently strongly acyclic

0, 0, 0

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Implementing Numbering of Leafs

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```

root:  pre[0] := 0
       pre[1] := pre[0]
       post[0] := post[1]
    
```

```

node:  pre[1] := pre[0]
       pre[2] := post[1]
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```

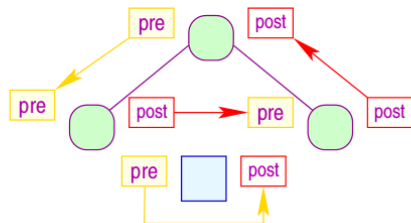
```

leaf:  post[0] := pre[0] + 1
    
```

Handwritten red annotations: a bracket on the right side of the root definitions, an arrow pointing to the right, and the word "SINCE" written vertically.

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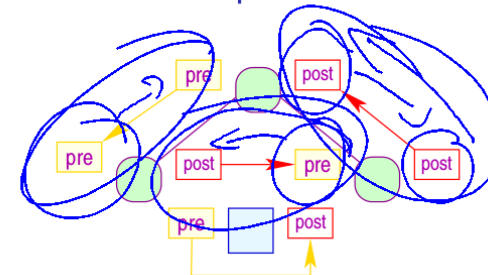
The Local Attribute Dependencies



- the attribute system is apparently strongly acyclic

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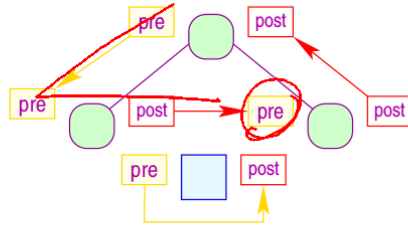
The Local Attribute Dependencies



- the attribute system is apparently strongly acyclic
- each node computes
 - the inherited attributes before descending into a child node (corresponding to a pre-order traversal)
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The Local Attribute Dependencies



- the attribute system is apparently strongly acyclic
- each node computes
 - the inherited attributes before descending into a child node (corresponding to a pre-order traversal)
 - the synthetic attributes after returning from a child node (corresponding to post-order traversal)
- if all attributes can be computed in a *single* depth-first traversal that proceeds from left- to right (with pre- and post-order evaluation)
- then we call this attribute system *L-attributed*.

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L-attributed

Definition

An attribute system is *L-attributed*, if for all productions $s ::= s_1 \dots s_n$ every inherited attribute of s_j where $1 \leq j \leq n$ only depends on

- 1 the attributes of s_1, s_2, \dots, s_{j-1} and
- 2 the inherited attributes of s .

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Origin:

- the attributes of an *L-attributed* grammar can be evaluated during parsing
- important if no syntax tree is required or if error messages should be emitted while parsing
- example: pocket calculator

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L-attributed grammars have a fixed evaluation strategy: a *single depth-first traversal*

- in general: partition all attributes into $\mathcal{A} = A_1 \cup \dots \cup A_n$ such that for all attributes in A_i the attribute system is *L-attributed*
- perform a *depth-first* traversal for each attribute set A_i

↪ craft attribute system in a way that they can be partitioned into few *L-attributed* sets

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Practical Applications

- symbol tables, type checking/inference, and simple code generation can all be specified using L -attributed grammars

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Practical Applications

- symbol tables, type checking/inference, and simple code generation can all be specified using L -attributed grammars
- most applications *annotate* syntax trees with additional information
- the nodes in a syntax tree often have different *types* that depends on the non-terminal that the node represents
- the different types of non-terminals are characterised by the set of attributes with which they are decorated

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Implementation of Attribute Systems via a *Visitor*

- class with a method for every non-terminal in the grammar
- attribute-evaluation works via *pre-order / post-order callbacks*

```
public abstract class Regex {
    public abstract void accept(Visitor v);
}

public interface Visitor {
    default void pre(OrEx re) {}
    default void pre(AndEx re) {}
    ...
    default void post(OrEx re) {}
    default void post(AndEx re){}
}

public class OrEx extends Regex {
    Regex l, r;
    public void accept(Visitor v) {
        v.pre(this); l.accept(v); v.inter(this);
        r.accept(v); v.post(this);
    }
}
```

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Example: Leaf Numbering

```
public abstract class AbstractVisitor
implements Visitor {
    default void pre(OrEx re) { pr(re); }
    default void pre(AndEx re) { pr(re); }
    ...
    default void post(OrEx re) { po(re); }
    default void post(AndEx re){ po(re); }
    abstract void po(BinEx re);
    abstract void in(BinEx re);
    abstract void pr(BinEx re);
}

public class LeafNum extends Visitor {
    public LeafNum(Regex r) { n.set(r,0);r.accept(this); }
    public Map<Regex,Integer> n = new HashMap<>();
    public void pr(Const r) { n.set(r, n.get(r)+1); }
    public void pr(BinEx r) { n.set(r.l,n.get(r)); }
    public void in(BinEx r) { n.set(r.r,n.get(r.l)); }
    public void po(BinEx r) {
        n.set(r,n.get(r.l)+n.get(r.r));
    }
}
```

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public class OrEx extends Regex {
    Regex l, r;
    public void accept(Visitor v) {
        v.pre(this); l.accept(v); v.inter(this);
        r.accept(v); v.post(this);
    }
}
```

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Semantic Analysis

Chapter 2: Symbol Tables

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Symbol Tables

Consider the following Java code:

```
void foo() {
    int A;
    void bar() {
        double A;
        A = 0.5;
        write(A);
    }
    A = 2;
    bar();
    write(A);
}
```

- within the body of `bar` the definition of `A` is shadowed by the *local definition*
- each *declaration* of a variable `v` requires the compiler to set aside some memory for `v`; in order to perform an access to `v`, we need to know to which declaration the access is *bound*
- we consider only *static allocation*, where the memory is allocated while a variable is *in scope*
- a binding is not *visible* within local declaration of the same name is in scope

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Scope of Identifiers

```
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    int A;
    void bar() {
        double A;
        A = 0.5;
        write(A);
    }
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    bar();
    write(A);
}
```

} scope of `int A`

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    A = 2;
    bar();
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}
```

} administration of identifiers can be quite complicated...

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Visibility Rules in Object-Oriented Languages

```

1 public class Foo {
2     int x = 17;
3     protected int y = 5;
4     private int z = 42;
5     public int b() { return 1; }
6 }
7 class Bar extends Foo {
8     protected double y = 0.5;
9     public int b(int a)
10        { return a+x; }
11 }

```

Modifier	Class	Package	Subclass	World
public	✓	✓	✓	✓
protected	✓	✓	✓	✗
no modifier	✓	✓	✗	✗
private	✓	✗	✗	✗

Observations:

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Observations:

- private member `z` is only visible in methods of class `Foo`
- protected member `y` is visible in the same package and in sub-class `Bar`, but here it is *shadowed* by `double y`
- `Bar` does not compile if it is not in the same package as `Foo`
- methods `b` with the same name are different if their arguments differ \leadsto *static overloading*

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Dynamic Resolution of Functions

```

1 public class Foo {
2     protected int foo() { return 1; }
3 }
4 class Bar extends Foo {
5     protected int foo() { return 2; }
6     public int test(boolean b) {
7         Foo x = (b) ? new Foo() : new Bar();
8         return x.foo();
9     }
10 }

```

Observations:

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```

Observations:

- the type of `x` is `Foo` or `Bar`, depending on the value of `b`
- `x.foo()` either calls `foo` in line 2 or in line 5
- this decision is made at *run-time* and has nothing to do with name resolution

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Resolving Identifiers

Observation: each identifier in the AST must be translated into a memory access

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Observation: each identifier in the AST must be translated into a memory access

Problem: for each identifier, find out what memory needs to be accessed by providing *rapid* access to its *declaration*

Idea:

- 1 *rapid* access: replace every identifier by a *unique* “name”, namely an integer
 - integers as keys: comparisons of integers is faster
 - replacing various identifiers with number saves memory

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Idea:

- 1 *rapid* access: replace every identifier by a *unique* “name”, namely an integer
 - integers as keys: comparisons of integers is faster
 - replacing various identifiers with number saves memory
- 2 link each usage of a variable to the *declaration* of that variable
 - track data structures to distinguish declared variables and visible variables
 - for languages without explicit declarations, create declarations when a variable is first encountered

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(1) Replace each Occurrence with a Number

Rather than handling strings, we replace each string with a unique number.

Idea for Algorithm:

Input: a sequence of strings

Output:

- 1 sequence of numbers
- 2 table that allows to retrieve the string that corresponds to a number

Apply this algorithm on each identifier in the *scanner*.

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Example for Applying this Algorithm

Input:

0	1	2	3	4	5	6	7	
Peter	Piper	picked	a	peck	of	pickled	peppers	
8	0	1	2					
If	Peter	Piper	picked	a	peck	of	pickled	peppers
wheres	the	peck	of	pickled	peppers	Peter	Piper	picked

Output:

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Input:

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Output:

0	1	2	3	4	5	6	7	8	0	1	2	3	4	5	6
7	9	10	4	5	6	7	0	1	2						

and

0	Peter
1	Piper
2	picked
3	a
4	peck
5	of

6	pickled
7	peppers
8	If
9	wheres
10	the

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Implementing the Algorithm: Specification

Idea:

- implement a *partial map*: $S : \text{String} \rightarrow \text{int}$
- use a counter variable `int count = 0`; to track the number of different identifiers found so far

We thus define a function `int getIndex(String w)`:

```
int getIndex(String w) {
    if (S(w) ≡ undefined) {
        S = S ⊕ {w ↦ count};
        return count++;
    } else return S(w);
}
```

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Data Structures for Partial Maps

possible data structures:

- list of pairs $(w, i) \in \text{String} \times \text{int}$:
 - insert: $\mathcal{O}(1)$
 - lookup: $\mathcal{O}(n)$ \rightsquigarrow too expensive \times

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- balanced trees :
insert: $\mathcal{O}(\log(n))$
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insert: $\mathcal{O}(1)$
lookup: $\mathcal{O}(1)$ on average ✓

caveat: we will see that the handling of scoping requires additional operations that are hard to implement with hash tables

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An Implementation using Hash Tables

- allocated an array M of sufficient size m
- choose a *hash function* $H : \text{String} \rightarrow [0, m - 1]$ with the following properties:
 - $H(w)$ is *cheap* to compute
 - H distributes the occurring words *equally* over $[0, m - 1]$

Possible choices ($\vec{x} = \langle x_0, \dots, x_{r-1} \rangle$):

$$\begin{aligned} H_0(\vec{x}) &= (x_0 + x_{r-1}) \% m \\ H_1(\vec{x}) &= \left(\sum_{i=0}^{r-1} x_i \cdot p^i \right) \% m \\ &= (x_0 + p \cdot (x_1 + p \cdot (\dots + p \cdot x_{r-1} \dots))) \% m \end{aligned}$$

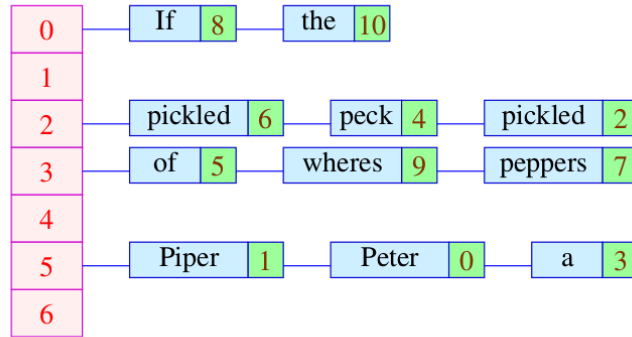
for some prime number p (e.g. 31)

- We store the pair (w, i) in a linked list located at $M[H(w)]$

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Computing a Hash Table for the Example

With $m = 7$ and H_0 we obtain:



In order to find the index for the word w , we need to compare w with all words x for which $H(w) = H(x)$

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Resolving Identifiers: (2) Symbol Tables

Check for the correct usage of variables:

- Traverse the syntax tree in a suitable sequence, such that
 - each definition is visited **before** its use
 - the currently visible definition is the last one visited
- for each identifier, we manage a **stack** of scopes
- if we visit a **declaration** of an identifier, we push it onto the stack
- upon leaving the **scope**, we remove it from the stack
- if we visit a **usage** of an identifier, we pick the top-most declaration from its stack
- if the stack of the identifier is empty, we have found an error

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Example: A Table of Stacks

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Example: A Table of Stacks

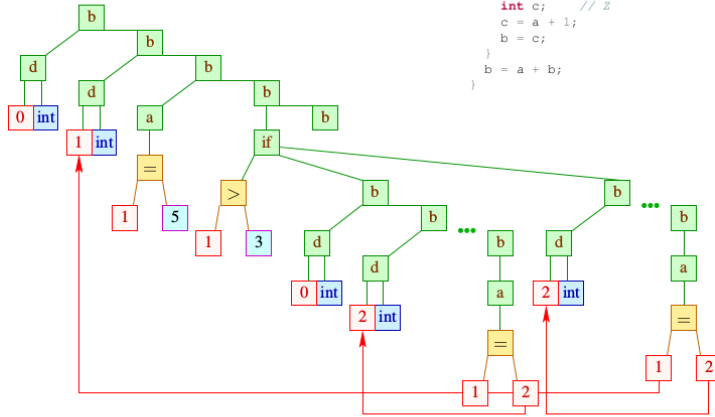
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Resolving: Rewriting the Syntax Tree

- d declaration node
- b basic block
- a assignment

```

int a, b; // V, W
b = 5;
if (b > 3) {
    int a, c; // X, Y
    a = 3;
    c = a + 1;
    b = c;
} else {
    int c; // Z
    c = a + 1;
    b = c;
}
b = a + b;
    
```

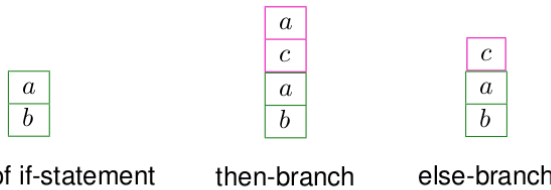


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 - equation system for basic block must add and remove identifiers

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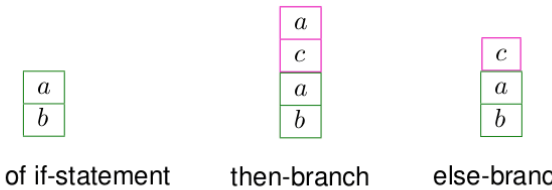
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Alternative Resolution of Visibility

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- instead of lists of symbols, it is possible to use a list of hash tables ~> more efficient in large, shallow programs
- a more elegant solution is to use a *persistent tree* in which an update returns a new tree but leaves all old references to the tree unchanged
 - a persistent tree t can be passed down into a basic block where new elements may be added; after examining the basic block, the analysis proceeds with the unchanged t

Forward Declarations

Most programming language admit the definition of recursive data types and/or recursive functions.

- a recursive definition needs to mention a name that is currently being defined or that will be defined later on
- old-fashion programming languages require that these cycles are broken by a *forward* declaration